

## Fermat and the Circle

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The Binomial Expansion yields the result:

$$c^n = a^n + b^n + \text{rem}(a,b,n) \text{ where } \text{rem}(a,b,n) > 0$$

This by itself proves Fermat's Theorem for a,b, and c integers and  $n > 2$

(for  $n = 2$ , the expression can be that of a circle if a,b,c form a Pythagorean triple; otherwise the Binomial Theorem applies.

If Fermat's expression were true,  $c^n = a^n + b^n$ , it would mean that  $\text{rem}(a,b,n) = 0$ .

Since  $\text{Rem}(a,b,n)$  consists of additive terms which are all composed of multiplicative products of a and b (e.g.  $a^n b^m$ ), it can only vanish if  $a=0$  or  $b=0$ , so that  $c^n = b^n$  or  $c^n = a^n$ , respectively.

Since the Binomial Theorem is valid all numbers (e.g. fractions, transcendentals, and complex numbers), the question of whether a and b are integers is moot - it is the remainder term that must vanish.

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For the relativistic circle in two dimensions (a,b) positive numbers are generated in the positive quadrant of the circle by the prescription  $\gamma=1$  when  $\beta=0$ , and vice versa, so that

$$n = n\gamma \text{ or } m = m\beta \text{ at } \theta=0 \text{ or } \theta = \frac{\pi}{2} \text{ at } v=c, \text{ respectively.}$$

(for  $v=0$ ,  $\gamma=1$ ,  $\gamma = \frac{1}{\sqrt{1-\beta^2}}$ ,  $\beta = \frac{v}{c}$ , but at  $\theta=0$ ,  $\beta = 0$ ,  $\gamma=1$ , so  $a = a\gamma$  for each integer generated represented by a, and  $na = na\gamma$  .

(for  $v = c$ ,  $\gamma=0$ ,  $\beta=1$ , and  $b = b\beta$  for each integer b.

The product  $\beta\gamma$  can be thought of as the area of either a concentric circle or the diagonal of an inscribed polygon, where the area of its equivalent square is  $\sqrt{2}$

For  $\beta < 1$ , the product  $\gamma\beta$  cannot be an integer, since  $(\gamma\beta) < 1^2$ , corresponding to the result

of the Binomial Expansion of  $n(1^n) = n(\gamma^n + \beta^n)$  , since  $1^2 = \gamma^2 + \beta^2$

For  $\beta > 1$  the corresponding expression is  $\gamma^2 = 1^2 + (\beta\gamma)^2$  which can only be valid for  $\gamma = 1$  and  $\beta\gamma = 0$  (i.e.,  $\beta = 0$ )

(For QFT, it is instructive to think of  $\beta = h$  and/or  $\gamma = h$  , where h is Planck's constant).